Circle

Question 1.

Calculate the length of a chord which is at a distance of 12 cm from the centre of a circle of radius 13 cm.

Solution:

AB is chord of a circle with centre O and OA is its radius OM \perp AB.



Question 2.

A chord of length 48 cm is drawn in a circle of radius 25 cm. Calculate its distance from the centre of the circle. Solution:

AB is the chord of the circle with centre O and radius OA and OM \perp AB.



Question 3.

A chord of length 8 cm is at a distance of 3 cm from the centre of the circle. Calculate the radius of the circle. Solution:

AB is the chord of a circle with centre O and radius OA and OM \perp AB



Question 4.

Calculate the length of the chord which is at a distance of 6 cm from the centre of a circle of diameter 20 cm.

Solution:

AB is the chord of the circle with centre O and radius OA and OM \perp AB



$$\therefore$$
 Radius = $\frac{20}{2}$ = 10 cm

 \therefore OA = 10 cm, OM = 6 cm

Now in right Δ OAM,

$$OA^2 = AM^2 + OM^2$$

(By Pythagorus Axiom)

$$\Rightarrow (10)^2 = AM^2 + (6)^2$$

$$\Rightarrow AM^2 = 10^2 - 6^2$$

$$\Rightarrow AM^2 = 100 - 36 = 64 = (8)^2$$

- ∴ AM = 8 cm
- \therefore OM \perp AB
- \therefore M is the mid-point of AB.
- $\therefore AB = 2 AM = 2 \times 8 = 16 cm.$

Question 5.

A chord of length 16 cm is at a distance of 6 cm from the centre of the circle. Find the length of the chord of the same circle which is at a distance of 8 cm from the centre.

Solution:



Question 6.

In a circle of radius 5 cm, AB and CD are two parallel chords of length 8 cm and 6 cm respectively. Calculate the distance between the chords if they are on : (i) the same side of the centre.

(ii) the opposite sides of the centre. Solution:

Two chords AB and CD of a circle with centre O and radius OA or OC



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In right
$$\triangle OAM$$
,
 $OA^2 = AM^2 + OM^2$
(By Pythagorus Axiom)
 $\Rightarrow (5)^2 = (4)^2 + OM^2$
 $\left(\because AM = \frac{1}{2}AB\right)$
 $\Rightarrow 25 = 16 + OM^2$
 $\Rightarrow OM^2 = 25 - 16 = 9 = (3)^2$
 $\therefore OM = 3 \text{ cm.}$
Again in right $\triangle OCN$,
 $OC^2 = CN^2 + ON^2$
 $\Rightarrow (5)^2 = (3)^2 + ON^2$
 $\left(\because CN = \frac{1}{2}CD\right)$
 $\Rightarrow 25 = 9 + ON^2$
 $\Rightarrow ON^2 = 25 - 9 = 16 = (4)^2$
 $\therefore ON = 4$
In fig. (*i*), distance MN = ON - OM
 $= 4 - 3 = 1 \text{ cm.}$
In fig. (*ii*)

MN = OM + ON = 3 + 4 = 7 cm

Question 7.

(a) In the figure given below, O is the centre of the circle. AB and CD are two chords of the circle, OM is perpendicular to AB and ON is perpendicular to CD. AB = 24 cm, OM = 5 cm, ON = 12 cm. Find the:

- (i) radius of the circle.
- (ii) length of chord CD.



(b) In the figure (ii) given below, CD is the diameter which meets the chord AB in

E such that AE = BE = 4 cm. If CE = 3 cm, find the radius of the circle.



Solution:

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Question 8.

In the adjoining figure, AB and CD ate two parallel chords and O is the centre. If the radius of the circle is 15 cm, find the distance MN between the two chords of length 24 cm and 18 cm respectively.



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Question 9.

AB and CD are two parallel chords of a circle of lengths 10 cm and 4 cm respectively. If the chords lie on the same side of the centre and the distance between them is 3 cm, find the diameter of the circle. Solution:

AB and CD are two parallel chords and AB



Question 10.

ABC is an isosceles triangle inscribed in a circle. If AB = AC = $12\sqrt{5}$ cm and BC = 24 cm, find the radius of the circle. Solution:

 $AB = AC = 12\sqrt{5}$ and BC = 24 cm. Join OB and OC and OA. Draw AD \perp BC which will pass through centre O. .: OD bisects BC in D \therefore BD = DC = 12 cm. In right ∆ABD $AB^2 = AD^2 + BD^2$ $\Rightarrow (12\sqrt{5})^2 = AD^2 + (12)^2$ \Rightarrow 144 × 5 = AD² + 144 \Rightarrow 720 - 144 = AD² \Rightarrow AD² = 576 \Rightarrow AD = $\sqrt{576}$ = 24 Let radius of the circle = OA = OB = OC = r \therefore OD = AD - AO = 24 - r Now in right $\triangle OBD$, $OB^2 = BD^2 + OD^2$ $\Rightarrow r^2 = (12)^2 + (24 - r)^2$ $\Rightarrow r^2 = 144 + 576 + r^2 - 48 r$ \Rightarrow 48 r = 720 $r = \frac{720}{48} = 15 \,\mathrm{cm}.$.: Radius = 15 cm

Question 11.

An equilateral triangle of side 6 cm is inscribed in a circle. Find the radius of the circle.

Solution:

ABC is an equilateral triangle inscribed in a circle with centre O. Join OB and OC.

From A, draw AD \perp BC which will pass through the centre O of the circle.



 \therefore Each side of $\triangle ABC = 6$ cm.

$$\therefore \quad AD = \frac{\sqrt{3}}{2}a = \frac{\sqrt{3}}{2} \times 6 = 3\sqrt{3} \text{ cm.}$$
$$OD = AD - AO = 3\sqrt{3} - r.$$

Now in right $\triangle OBD$,

$$OB^{2} = BD^{2} + OD^{2}$$

$$\Rightarrow r^{2} = (3)^{2} + (3\sqrt{3} - r)^{2}$$

$$\Rightarrow r^{2} = 9 + 27 + r^{2} - 6\sqrt{3}r$$
(. D is mid-point of BC)

$$6\sqrt{3}r = 36$$

$$r = \frac{36}{6\sqrt{3}} = \frac{6 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} = \frac{6\sqrt{3}}{3} = 2\sqrt{3} \text{ cm}$$

$$\therefore$$
 Radius = $2\sqrt{3}$ cm

Question 12.

AB is a diameter of a circle. M is a point in AB such that AM = 18 cm and MB = 8 cm. Find the length of the shortest chord through M. Solution:

In a circle with centre O, AB is the diameter and M is a point on AB such that



Question 13.

A rectangle with one side of length 4 cm is inscribed in a circle of diameter 5 cm. Find the area of the rectangle.

Solution:

ABCD is a rectangle inscribed in a circle with centre O and diameter 5 cm.



$$AB = 4 \text{ cm} \text{ and } AC = 5 \text{ cm}.$$

In right $\triangle ABC$,

- $AC^2 = AB^2 + BC^2$
- $\Rightarrow (5)^2 = (4)^2 + BC^2 \Rightarrow BC^2 = 5^2 4^2$
- $\Rightarrow BC^2 = 25 16 = 9 = (3)^2$
- \therefore BC = 3 cm.
- \therefore Area of rectangle ABCD = AB × BC

$$= 4 \times 3 = 12 \text{ cm}^2$$

Question 14.

The length of the common chord of two intersecting circles is 30 cm. If the radii of the two circles are 25 cm and 17 cm, find the distance between their centres. Solution:

AB is the common chord of two circles with centre O and C. Join OA, CA and OC



Question 15.

The line joining the mid-points of two chords of a circle passes through its centre. Prove that the chords are parallel. Solution:

Given : Two chords AB and CD where L and M are the mid-points of AB and CD respectively. LM passes through O, the centre of the circle.



To Prove : AB || CD.

Proof : ... L is mid-point of AB.

∴ OL⊥AB

 $\therefore \angle OLA = 90^{\circ}$...(*i*)

Again M is mid point of CD

- \therefore OM \perp CD
- $\therefore \angle OMD = 90^{\circ}$...(*ii*)

From (i) and (ii)

∠OLA = ∠OMD

But these are alternate angles

 \therefore AB || CD Q.E.D.

Question 16.

If a diameter of a circle is perpendicular to one of two parallel chords of the circle, prove that it is perpendicular to the other and bisects it. Solution:

Given : Chord AB || CD

and diameter PQ is perpendicular to AB



To Prove : PQ is perpendicular to CD.

Proof : ... Diameter PQ is perpendicular to AB.

∴ ∠AMO = 90°

∴ PQ bisects AB

 \therefore AB || CD (given)

 $\therefore \angle OLD = 90^{\circ}$ (Alt. angles)

: OL or PQ is perpendicular to CD.

Hence PQ bisects CD. Q.E.D.

Question 17.

In an equilateral triangle, prove that the centroid and the circumcentre of the triangle coincide.

Solution:

Given : $\triangle ABC$ in which AB = BC = CA.

To Prove : The centroid and the circumcentre coincide each other.

Construction : Draw perpendicular bisectors of AB and BC intersecting each other at O. Join AD, OB and OC.

Proof : \therefore O lies on the perpendicular bisectors of AB and BC

 \therefore OA = OB = OC

 \therefore O is the cimcumcentre of \triangle ABC.

·. D is mid-point of BC.

 \therefore AD is the median of \triangle ABC.

Now in $\triangle ABD$ and $\triangle ACD$,

AB = AC	(given)
AD = AD	(common)
BD = BC	(·. D is mid-point of BC)

∴ ΔABD ≅ ΔACD

(SSS axiom of congruency)

 $\therefore \ \angle ADB = \angle ADC \qquad (c.p.c.t)$

But $\angle ADB + \angle ADC = 180^{\circ}$

(Linear pair)

 $\therefore \ \angle ADB = \angle ADC = 90^{\circ}$

 \therefore AD is perpendicular on BC which passes through O.

Hence centroid and circumcentre of $\triangle ABC$ coincide each other. Q.E.D.

Question 18.

(a) In the figure (i) given below, OD is perpendicular to the chord AB of a circle whose centre is O. If BC is a diameter, show that CA = 2 OD.
(b) In the figure (ii) given below, O is the centre of a circle. If AB and AC are

chords of the circle such that AB = AC and $OP \perp AB$, $OQ \perp AC$, Prove that PB = QC.

Solution:

(a) Given : OD is perpendicular to chord

AB of the circle and BOC is the diameter.

CA is joined.

To Prove : CA = 2 OD.

Proof : \because OD \perp AB

 \therefore D is mid point of AB and O is the mid point of BC.

∴ In ∆BAC,

OD || CA and OD =
$$\frac{1}{2}$$
CA
 \Rightarrow CA = 2 OD Q.E.D.

(b) Given : AB and AC are chords of a circle with centre O and AB = AC, OP \perp AB and OQ \perp AC. BP and QC are joined.

To Prove : PB = QC. Proof : \therefore OP \perp AB (given) \therefore M is mid-point of AB \therefore AM = MB \Rightarrow MB = $\frac{1}{2}$ AB

Similarly $OQ \perp AC$

$$\therefore \quad AN = NC \implies NC = \frac{1}{2}AC.$$

ButAB = AC

- \therefore MB = NC
- : Chord AB = Chord AC
- \therefore OM = ON

But OP = OQ (radii of the same circle)

 \therefore MP = NQ

Now in \triangle MPB and \triangle NQC,

$$MB = NC$$
 (proved)

$$MP = NQ$$
 (proved)
∠PMB = ∠QNC (each 90°)
∴ ΔMPB ≅ ΔNQC

(SAS axiom of congruency)

 \therefore PB = QC (c.p.c.t) Q.E.D

Question 19.

(a) In the figure (i) given below, a line I intersects two concentric circles at the points A, B, C and D. Prove that AB = CD.

(b) In the figure (it) given below, chords AB and CD of a circle with centre O intersect at E. If OE bisects $\angle AED$, Prove that AB = CD.

Solution:

(a) Given : A line l intersects two concentric circles with centre O.

To Prove : AB = CD

Construction : Draw OM $\perp l$.

Q.E.D. :

(b) Given : Two chords AB and CD intersect each other at E inside the circle with centre O. OE bisects ∠AED *i.e.* ∠OEA = ∠OED. To Prove : AB = CD Construction : From O, draw OM \perp AB and ON \perp CD. **Proof** : In $\triangle OME$ and $\triangle ONE$ (each 90°) $\angle M = \angle N$ м (common) OE = OE(given) ∠OEM = ∠OEN $\therefore \Delta OME \cong \Delta ONE$ (ASS axiom of congruency) OM = ON... AB = CD.:. (chords which are equidistant from the centre are equal) Q.E.D.

Question 20.

(a) In the figure (i) given below, AD is a diameter of a circle with centre O. If AB || CD, prove that AB = CD.

(b) In the figure (ii) given below, AB and CD are equal chords of a circle with centre O. If AB and CD meet at E (outside the circle) Prove that :
(i) AE = CE (ii) BE = DE.

Solution:

(a) Given : AD is the diameter of a circle with centre O and chords AB and CD are parallel.

To Prove : AB = CD.

Construction : From O, draw OM \perp AB and ON \perp CD

Proof : In $\triangle OMA$ and $\triangle OND$,

∠AOM = ∠DON

(Vertically opposite angles)

OA = OD (radii of the same circle) and $\angle M = \angle N$ (each 90°)

∴ ΔOMA ≅ ΔOND

(AAS axiom of congruency)

$$\therefore OM = ON$$
 (c.p.c.t)

But OM \perp AB and ON \perp CD

$$\therefore$$
 AB = CD

(chords which are equidistant from the centre are equal)

(b) Given : Chord AB = chord CD of circle with centre O. and meet at E on producing them.

To Prove : (i) AE = CE(ii) BE = DEConstruction : From O, draw $OM \perp AB$ and $ON \perp CD$. Join OEIn right $\triangle OME$ and $\triangle ONE$ Hyp. OE = OE (Common) Side OM = ON

(Equal chords are equidistant from the centre)

 $\therefore \Delta OME \cong \Delta ONE$

(R.H.S. axiom of congruency)

 $\therefore ME = NE \qquad (c.p.c.t) \dots (i)$

 \therefore OM \perp AB and ON \perp CD

 \therefore M is mid-point of AB and N is mid point of CD.

$$MB = \frac{1}{2}AB \text{ and } ND = \frac{1}{2}CD$$
But $AB = CD$...(*ii*)

$$MB = ND$$

$$Subtracting, (ii) from (i)
$$ME - MB = NE - ND$$

$$BE = DE$$
But $AB = CD$ (given)

$$Adding, we get$$

$$AB + BE = CD + DE$$

$$AE = CE$$
 (Hence proved)$$

EXERCISE 15.2

Question 1.

If arcs APB and CQD of a circle are congruent, then find the ratio of AB: CD. Solution:

 $\overrightarrow{APB} = \overrightarrow{CQD}$ (given)

 $\therefore AB = CD$

(: If two arcs are congruent, then their corresponding chords are equal)

- \therefore Ratio of AB and CD = $\frac{AB}{CD} = \frac{AB}{AB} = \frac{1}{1}$
- \Rightarrow AB : CD = 1 : 1

Question 2.

A and B are points on a circle with centre O. C is a point on the circle such that OC bisects $\angle AOB$, prove that OC bisects the arc AB. Solution:

Given : In a given circle with centre O, A and B are two points on the circle. C i^o another point on the circle such that $\angle AOC = \angle BOC$

To prove : arc AC = arc BC **Proof :** \therefore OC is the bisector of $\angle AOB$ or $\angle AOC = \angle BOC$ But these are the angle subtended by the arc AC and BC.

 \therefore arc AC = arc BC. Q.E.D.

Question 3.

Prove that the angle subtended at the centre of a circle is bisected by the radius

passing through the mid-point of the arc. Solution:

Since : All is its un al die singe thie ander Gaal Chainsteingelie alsonalit. To ware : All lingen die Althu

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- $\therefore \angle AOC = \angle BOC$

Hence OC bisects the $\angle AOB$. Q.E.D.

Question 4.

In the given figure, two chords AB and CD of a circle intersect at P. If AB = CD, prove that arc AD = arc CB. Solution:

Given : Two chords AB and CD of a circle intersect at P and AB = CD. To prove : arc AD = arc CB Proof : AB = CD (given)

- minor arc AB = minor arc CD
 Subtracting arc BD from both sides
 arc AB arc BD = arc CD arc BD
- \Rightarrow arc AD = arc CD Q.E.D.

Multiple Choice Questions

Choose the correct answer from the given four options (1 to 6) : **Question 1**.

If P and Q are any two points on a circle, then the line segment PQ is called a (a) radius of the circle

(b) diameter of the circle

- (c) chord of the circle
- (d) secant of the circle

Solution:

chord of the circle (c)

Question 2.

If P is a point in the interior of a circle with centre O and radius r, then (a) OP = r(b) OP > r(c) $OP \ge r$ (d) OP < rSolution: OP > r (b)

Question 3.

The circumference of a circle must be (a) a positive real number (b) a whole number (c) a natural number (d) an integer Solution: a positive real number (a)

Question 4.

AD is a diameter of a circle and AB is a chord. If AD = 34 cm and AB = 30 cm, then the distance of AB from the centre of circle is

- (a) 17 cm
- (b) 15 cm
- (c) 4 cm
- (d) 8 cm

Solution:

AD is the diameter of the circle whose length is AD = 34 cm

AB is the chord of the circle whose length is AB = 30 cm

Distance of the chord from the centre is OM Since the line through the centre of the chord of the circle is the perpendicular bisector, we have $\angle OMA = 90^{\circ}$

and AM = BM

Thus, ΔAMO is a right angled triangle

Now, by applying Pythagorean Theorem,

 $OA^2 = AM^2 + OM^2$

Since the diameter AD = 34 cm, radius of the circle is 17 cm

... We have AM = BM = 15 cmWe have, $OA^2 = AM^2 + OM^2$ $17^2 = 15^2 + OM^2$ $OM^2 = 289 - 225$ $OM^2 - 64$ $OM = \sqrt{64} = 8 \text{ cm}$

(d)

...(i)

Question 5.

If AB = 12 cm, BC = 16 cm and AB is perpendicular to BC, then the radius of the circle passing through the points A, B and C is

(a) 6 cm (b) 8 cm

- (c) 10 cm
- (d) 12 cm

Solution:

Give that AB = 12 cm and BC = 16 cm and $\angle ABC = 90^{\circ}$

Every angle inscribed in a semicircle is a right angle.

Since the inscribed angle

 $\angle ABC = 90^{\circ}$, the arc ABC is a semicircle

Thus, AC is the diameter of the circle passing through the centre.

Now, by Pythagoras Theorem,

$$AC^{2} = AB^{2} + BC^{2}$$

= $12^{2} + 16^{2}$
= $14 + 256 = 400$
 $AC = \sqrt{400} = 20 \text{ cm}$

Diameter of the circle is 20 cm
 Thus, the radius of the circle passing through
 A, B and C is 10 cm. (c)

Question 6.

In the given figure, O is the centre of the circle. If OA = 5 cm, AB = 8 cm and OD \perp AB, then length of CD is equal to

- (a) 2 cm
- (b) 3 cm
- (c) 4 cm
- (d) 5 cm
- Solution:

$$=\sqrt{25-16} = \sqrt{9}$$
 cm = 3 cm

Since, OD = OA = 5 cm

 $\therefore CD = OD - OC = 5 - 3 cm = 2 cm$ (a)

Chapter Test

Question 1.

In the given figure, a chord PQ of a circle with centre O and radius 15 cm is bisected at M by a diameter AB. If OM = 9 cm, find the lengths of :

- (i) PQ (ii) AP
- (iii) AP

Solution:

Given, radius = 15 cm \Rightarrow OA = OB = OP = OQ = 15 cm Also, OM = 9 cm

:. MB = OB - OM = 15 - 9 = 6 cm AM = OA + OM = 15 + 9 cm = 24 cmIn $\triangle OMP$, by using Pythagoras Theoream,

OP² = OM² + PM²
15² = 9² + PM²
= PM² = 225 - 81
PM =
$$\sqrt{144}$$
 = 12 cm
Also, In Δ OMQ,
by using Pythagoras Theorem,
OQ² = OM² + QM²
15² = 0M² + QM²
15² = 9² + QM² \Rightarrow QM² = 225 - 81
QM = $\sqrt{144}$ = 12 cm
 \therefore PQ = PM + QM
(As radius is bisected at M)
 \Rightarrow PQ = 12 + 12 cm = 24 cm
(*ii*) Now in Δ APM
AP² = AM² + OM²
AP² = 24² + 12²
AP² = 576 + 144
AP = $\sqrt{720}$ = 12 $\sqrt{5}$ cm
(*iii*) Now in Δ BMP
BP² = BM² + PM²
BP² = 36 + 144
BP = $\sqrt{180}$ = 6 $\sqrt{5}$ cm

Question 2.

The radii of two concentric circles are 17 cm and 10 cm ; a line PQRS cuts the larger circle at P and S and the smaller circle at Q and R. If QR = 12 cm, calculate PQ.

Solution:

A line PQRS intersects the outer circle at P and S and inner circle at Q and R. Radius of outer circle OP = 17 cm and radius of inner circle OQ = 10 cm.

QR = 12 cm From O, draw OM \perp PS

$$\therefore \qquad QM = \frac{1}{2}QR = \frac{1}{2} \times 12 = 6 \text{ cm}$$

In right $\triangle OQM$,

$$OQ^{2} = OM^{2} + QM^{2}$$

⇒ (10)² = OM² + (6)²
⇒ OM² = 10² - 6²
= 100 - 36 = 64 = (8)²
∴ OM = 8 cm
Now in right ΔOPM,
OP² = OM² + PM²
⇒ (17)² = (8)² + PM²
⇒ PM² = (17)² - (8)²
= 289 - 64 = 225 = (15)²

 $\therefore PM = 15 cm$

 $\therefore PQ = PM - QM = 15 - 6 = 9 \text{ cm}$

Question 3.

A chord of length 48 cm is at a distance of 10 cm from the centre of a circle. If another chord of length 20 cm is drawn in the same circle, find its distance from the centre of the circle.

Solution:

O is the centre of the circle Length of chord AB = 48 cm and chord CD = 20 cm

:.
$$AL = LB = \frac{48}{2} = 24 \text{ cm}$$

and $CM = MD = \frac{20}{2} = 10 \text{ cm}$
 $OL = 10 \text{ cm}$
Now in right ΔAOL
 $OA^2 = AL^2 + OL^2$ (Pythagoras Theorem)
 $\Rightarrow OA^2 = (24)^2 + (10)^2 = 576 + 100$
 $= 676 = (26)^2$
.: $OA = 26 \text{ cm}$
But $OC = OA$ (radii of the same circle)
.: $OC = 26 \text{ cm}$
Now in right ΔOCM
 $OC^2 = OM^2 + CM^2$
 $(26)^2 = OM^2 + (10)^2$
 $676 = OM^2 + 100 \Rightarrow OM^2 = 676 - 100$
 $\Rightarrow OM^2 = 576 = (24)^2$
.: $OM = 24 \text{ cm}$

Question 4.

(a) In the figure (i) given below, two circles with centres C, D intersect in points P, Q. If length of common chord is 6 cm and CP = 5 cm, DP = 4 cm, calculate the distance CD correct to two decimal places.

(a) Two circles with centre C and D intersect each other at P and Q. PQ is the common chord = 6 cm. The line joining the centres C and D bisects the chord PQ at M.

(b) In the figure (ii) given below, P is a point of intersection of two circles with centres C and D. If the st. line APB is parallel to CD, Prove that AB = 2 CD.

$$\therefore PM = MQ = \frac{6}{2} = 3 cm$$

Now in right $\triangle CPM$,

$$CP^{2} = CM^{2} + PM^{2}$$

$$\Rightarrow (5)^{2} = CM^{2} + (3)^{2} \Rightarrow 25 = CM^{2} + 9$$

$$\Rightarrow CM^{2} = 25 - 9 = 16 = (4)^{2}$$

$$\therefore$$
 CM = 4 cm

and in right ΔPDM ,

$$PD^{2} = PM^{2} + MD^{2}$$

⇒ (4)² = (3)² + MD² ⇒ 16 = 9 + MD²
⇒ MD² = 16 - 9 = 7
∴ MD = $\sqrt{7}$ = 2.65 cm

 $\therefore \quad CD = CM + MD = 4 + 2.65$

$$= 6.65 \text{ cm}$$

Solution:

(b) Given : Two circles with centre C and D intersect each other at P and Q. A straight line APB is drawn parallel to CD.

To Prove : AB = 2 CD.

Construction : Draw CM and DN perpendicular to AB from C and D.

Proof : $:: CM \perp AP$

 \therefore AM = MP or AP = 2 MP

and DN \perp PB

$$\therefore$$
 BN = PN or PB = 2 PN

Adding

$$AP + PB = 2 MP + 2 PN$$

$$\Rightarrow$$
 AB = 2 (MP + PN) = 2 MN

 \Rightarrow AB = 2 CD. Q.E.D.

Question 5.

(a) In the figure (i) given below, C and D are centres of two intersecting circles. The line APQB is perpendicular to the line of centres CD.Provethat:

(i) AP=QB

(ii) AQ = BP.

(b) In the figure (ii) given below, two equal chords AB and CD of a circle with centre O intersect at right angles at P. If M and N are mid-points of the chords AB and CD respectively, Prove that NOMP is a square.

Solution:

(a) Given : Two circles with centres C and D intersect each other. A line APQB is drawn perpendicular to CD at M.

To Prove : (i) AP = QB (ii) AQ = BP. Construction : Join AC and BC, DP and DQ.

Proof : (*i*) In right \triangle ACM and \triangle BCM

Hyp. AC = BC (radii of same circle)

Side CM = CM (common)

 $\therefore \Delta ACM \cong \Delta BCM$

(R.H.S. axiom of congruency)

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(b) Given : Two chords AB and CD intersect each other at P at right angle in the circle. M and N are mid-points of the chord AB and CD.

To Prove : NOMP is a square.

Proof : ... M and N are the mid-points of AB and CD respectively.

 \therefore OM \perp AB and ON \perp CD

and OM = ON

(: Equal chords are at equal distance from the centre)

÷.

 \therefore AB \perp CD

 \therefore OM \perp ON

Hence NOMP is a square.

Question 6.

In the given figure, AD is diameter of a circle. If the chord AB and AC are equidistant from its centre O, prove that AD bisects \angle BAC and \angle BDC. Solution:

Given : AB and AC are equidistant from its centre O So, AB = AC In \triangle ABD and \triangle ACD AB = AC (given) \angle B = \angle C (\because Angle in a semicircle is 90°) AD = AD (common)

 $\therefore \Delta ABD \cong \Delta ACD$ (SSS rule of congruency)

 \therefore AD bisects \angle BAC and \angle BDC